

Übungen in AlgGeo $\diamond$ Exercices en AlgGéo $\diamond$ T. E1 $\diamond$ II / 5

Probl. 1 Gauss–Jordan: • *Gauss–Jordan*:

$$\left| \begin{array}{cccc|c} 1x + 2y + 0z + 4w & = & 0 \\ 0x + 1y + 0z + 0w & = & 1 \\ 1x + 0y + 3z + 6w & = & 2 \\ 0x + 1y + 5z + 1w & = & 3 \end{array} \right|$$

Probl. 2 (a) $M_4 = \begin{pmatrix} 1 & 2 & 0 & 4 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 3 & 6 \\ 0 & 1 & 5 & 1 \end{pmatrix} \quad \det(M_4) = ?$

(b) $M_a = \begin{pmatrix} 1 & 2 & 0 & a \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 3 & 6 \\ 0 & 1 & 5 & 1 \end{pmatrix} \quad \det(M_a) = ?$

Probl. 3 $\vec{a} = \begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} 3 \\ y \\ 4 \end{pmatrix}$, $\{\vec{a}, \vec{b}, \vec{c}\}$ l.a. l.d., $y = ?$

Probl. 4 $M_1 = \begin{pmatrix} + & 2 & 1 & 3 & 5 \\ -1 & 4 & 1 & 2 & 4 \\ +1 & 8 & 1 & 1 & 6 \\ 0 & 16 & 1 & 0 & 11 \\ -1 & 32 & 1 & -1 & 18 \end{pmatrix}$, $M_2 = \begin{pmatrix} -1 & 2 & 1 & 3 & 5 \\ +1 & 4 & 1 & 2 & 4 \\ -1 & 8 & 1 & 1 & 6 \\ 0 & 16 & 1 & 0 & 11 \\ +1 & 32 & 1 & -1 & 18 \end{pmatrix}$

$\det(M_1 + M_2) = ?$